TECHNICAL PAPER NO. 43

Rainfall-Frequency Atlas of the Hawaiian Islands

for Areas to 200 Square Miles, Durations to 24 Hours, and Return Periods from 1 to 100 Years
U.S. DEPARTMENT OF COMMERCE
LUTHER H. HODGES, Secretary
WEATHER BUREAU
F. W. REICHELDERFER, Chief

TECHNICAL PAPER NO. 43

Rainfall-Frequency Atlas of the Hawaiian Islands

for Areas to 200 Square Miles, Durations to 24 Hours, and Return Periods from 1 to 100 Years

Prepared by
Cooperative Studies Section
Hydrologic Services Division
U.S. Weather Bureau for
Engineering Division
Soil Conservation Service
U.S. Department of Agriculture

WASHINGTON, D.C.
1962
RAINFALL-FREQUENCY ATLAS OF THE HAWAIIAN ISLANDS
for Areas to 200 Square Miles, Durations to 24 Hours, and Return Periods from 1 to 100 Years

1. INTRODUCTION

Authority. This report was prepared for the Soil Conservation Service to provide rainfall criteria for planning and design purposes in connection with its Watershed Protection and Flood Prevention Program (authorization: P.L. 566, 83d Congress, and as amended).

Accuracy of results. The rainfall-frequency data presented in this report are believed to be as accurate as available basic data and current statistical procedures permit. As time passes more data will become available through increases in length of record and probably in density of station networks. Better network planning may also be expected. More reliable estimates of rainfall-frequency data may be possible in the near future, say 10 years from now.

Acknowledgments. The project was under the general supervision of J. L. H. Paulhus, Chief of the Cooperative Studies Section of the Hydrologic Services Division, W. E. Hiatt, Chief. D. M. Hershfield directed the statistical investigations required for determining the rainfall-frequency data. J. F. Miller and L. L. Weiss investigated the meteorological aspects of the problem. D. I. Blumenstock, former Pacific Area Climatologist, Honolulu, provided some very useful information on the rainfall regimes of the Hawaiian Islands and some unpublished pertinent manuscripts. M. J. Brown, present Pacific Area Climatologist, and S. Price reviewed the manuscript and made several pertinent suggestions. W. E. Miller and N. S. Fosd supervised the collection and processing of basic data. Drafting was supervised by C. W. Gardner. Coordination with the Soil Conservation Service was maintained through H. O. Ogrosky, Chief, Hydrology Branch. Engineering Division.

2. RAINFALL REGIME

Knowledge of the geographic features of the Hawaiian Islands is required in order to understand the characteristics of their rainfall. The major islands of the Hawaiian chain are: Hawaii, Maui, Oahu, Kauai, Molokai, Kahoolawe, Lanai, and Nihiu. These islands are located in the mid-Pacific in the area 19°–22° N., 155°–160° W. This location places the islands in the northeast trade-wind belt on the southern side of the semi-permanent Pacific High cell. Their precipitation regimes are greatly influenced by the temperature inversion (increase of temperature with altitude) characteristic of the trade-wind belt.

The trade-wind inversion is formed by broad-scale subsidence of air from high altitudes in the eastern extremities of subtropical Highs. The descent of the subsiding air is halted by the low-level maritime air flowing equatorward. The inversion marks the boundary between the two strata, which flow horizontally in the same direction. The height of the base of the inversion may vary from about 1,000 to over 8,000 ft. above sea level. The air layer below the inversion is moist and contains a great deal of cloudiness (trade-wind cumulus). Above the inversion the air is warm and very dry. In order for heavy rains to occur over the islands the inversion must be very high or it must be destroyed.

The trade winds are the prevailing weather influence in all seasons. Frequent heavy showers are characteristic of the windward districts. In general, the 6-month period November–April has more rain than May–October. Monthly rainfall amounts may show a phenomenal range, and the amounts for a few days occasionally exceed the annual normals.

Another important precipitation factor is the topography of the islands. The topography
ranges from the relatively uniform elevation changes on the island of Hawaii to the irregular, rough, much dissected surface of Kauai. The highest elevations are on Hawaii, where Mauna Kea and Mauna Loa rise to nearly 14,000 ft. Mt. Haleakala on Maui is 10,025 ft. high; Kawaikini Peak on Kauai, 5,170 ft.; and Mt. Kaala on Oahu, 4,025 ft. Over half of the total area of the islands lies within 5 mi. of the shores. One-fourth of the area is above 4,500 ft.; and slightly over one-fourth is below 1,000 ft., which is where most of the population lives.

3. RAIN GAGE DISTRIBUTION

There are reported to be about 1300 rain gages on the islands. Most gages are privately owned and operated. No provision was made in the past for analysis or publication of records from such gages. Most gages are located at the lower elevations where most of the population is concentrated. About 90 percent of the gages are in areas of light to moderate rainfall, hence they tend to yield somewhat biased samplings. A complete and detailed history of Hawaiian rainfall stations has been published [1]. Few stations are equipped with recording gages. A large number of the nonrecording gages are read only after each storm, semiweekly, weekly, biweekly, monthly, or seasonally. Figure 1 shows the distribution of rainfall stations, both active and discontinued, with at least 5 years of record.

4. BASIC DATA

Station data. Table 1 groups the number of daily precipitation stations on each island by length of record as of 1959, the last complete

![Precipitation stations map]

Figure 1.—Precipitation stations
year for which data were available at the time of this study. A total of 287 stations which take precipitation observations once daily were used in the frequency analysis. The only recording-gage stations with usable records were Honolulu, Hilo, and Lihue. Honolulu had a 46-yr. record but the other two stations had but 8-yr. and 9-yr. records, respectively. Stations with records exceeding 19 yr., of which there were 159, were used to define the frequency relationships. Stations with records of less than 20 yr. were used only to define more accurately the 2-yr. regional pattern.

Time increments. Analysis of hundreds of station-years of rainfall data has produced reliable empirical factors for converting observational-day and clock-hour data into maximum 24- and 1-hr. rainfalls. The factor 1.13 was used throughout to convert observational-day (or clock-hour) rainfall amounts to maximum 24-hr. (or 1-hr.) rainfall values.

5. FREQUENCY ANALYSIS

Two types of data series. The partial-duration series, which includes all high values even though several may have occurred in the same year and none in some years, was required for this study. However, the processing of partial-duration data is very laborious. Furthermore, there is no theoretical basis for extrapolating these data beyond the length of record. For these reasons an alternate procedure was used. The annual maximum event was collected for each year to form the annual series. After analysis for frequency, the annual series statistics were converted to partial-duration statistics for corresponding return periods, and the rainfall-frequency maps presented in this report thus, in effect, represent the results of a partial-duration analysis. Table 2, based on

![Figure 2.—Duration-interpolation diagram](attachment:image.png)

a sample of 50 widely scattered stations in the United States, gives the empirical factors for converting the partial-duration series to the annual series for return periods up to 10 yr. The two types of data series show no appreciable differences for return periods greater than 10 yr.

Duration-interpolation diagram. The generalized depth-duration relation presented in figure 2 provides a means for computing rainfall depth for any duration between 1 and 24 hr. if the 1- and 24-hr. amounts for a particular return period are given. The generalization was obtained empirically from data for 200 U.S. Weather Bureau first-order stations, and is the same relation shown in "Rainfall-Frequency Atlas of the United States" [2]. Rainfall values for durations between 1 and

![Table 2.—Empirical factors for converting partial-duration series to annual series](attachment:image.png)

EXAMPLE: What are the 2-, 5-, and 10-yr. 24-hr. annual series values for the point at 19°30' N., 150°12' W.? From the maps of figures 1l, 1r, and 2t, the partial-duration values are estimated to be 8.4, 11.5, and 13.7 in., respectively. Multiplying by the above factors, the annual series values are 7.4, 11.0, and 12.6 in.
24 hr. are obtained by plotting the 1- and 24-hr. values for the same return period on the corresponding duration lines and laying a straightedge between the two points. Intersections of the straightedge and intermediate duration lines yield corresponding rainfall values. Tests with observational data for intermediate durations showed that the depth-duration diagram yielded reasonable values. The 30-min. rainfall values for a particular return period were obtained by multiplying the 1-hr. rainfall for that return period by 0.75. If durations shorter than 30 minutes are required, the average relationships between 30-min. and 5-, 10- and 15-min. rainfall amounts can be obtained from table 3.

**Table 3.** Average relationship between 30-minute rainfall and shorter duration rainfall for the same return period

<table>
<thead>
<tr>
<th>Duration (min.)</th>
<th>5</th>
<th>10</th>
<th>15</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ratio</td>
<td>0.37</td>
<td>0.57</td>
<td>0.72</td>
</tr>
<tr>
<td>Average error (percent)</td>
<td>8</td>
<td>7</td>
<td>5</td>
</tr>
</tbody>
</table>

**Return-period—interpolation diagram.** The return-period diagram of figure 3 is based on data from 200 Weather Bureau first-order stations and is identical to the diagram used in "Rainfall-Frequency Atlas of the United States" [2]. The spacing of the ordinates is partly empirical and partly theoretical. From 1 to 10 yr. it is entirely empirical, being based on free-hand curves drawn through plots of partial-duration series data. The spacing for return periods of 20 yr. and longer was based on the Gumbel procedure [3] for analyzing annual series data. The transition was smoothed subjectively between the 10- and 20-yr. return periods. If values between 2 and 100 yr. are read from the return-period diagram, then converted to annual series values and plotted on either Gumbel or log-normal probability paper, the points will very nearly define a straight line. The application of the Gumbel extreme-value procedure, which is supported by theory, is also supported by experience [4].

**Tests for secular trend.** The use of short-record data introduces the question of possible secular trend and biased sample. Routine tests with data from records of equal length but for different periods showed no trend. The use of short-record data thus appears justified.

**6. ISOPLOUVIAL MAPS**

**$\bar{x}$ and $s_N$ 24-hr. maps.** Because of the relatively large amount of 24-hr. data available and the relatively small standard error associated with the arithmetic mean, $\bar{x}$, of the annual maximum rainfalls (annual series), the $\bar{x}$ 24-hr. map was constructed first. ($\bar{x}$ is approximately equal to the 2.3-yr. value.) A preliminary standard deviation map was also prepared. The reliability of the latter was increased by adjusting its values on the basis of a smoothed coefficient-of-variation map. The adjustments were made only on the standard deviation map because this statistic is sensitive to anomalous events whereas the mean is affected only slightly. Also, the standard deviation values had been adjusted when required to a common 50-yr. record standard. Table 4 lists

**Table 4.** Factors for adjusting standard deviation to 50-yr. record

<table>
<thead>
<tr>
<th>Length of record (yr.)</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
</tr>
</thead>
<tbody>
<tr>
<td>Factors for increasing standard deviation</td>
<td>1.29</td>
<td>1.08</td>
<td>1.04</td>
<td>1.02</td>
</tr>
</tbody>
</table>
the empirical adjustment factors determined from 200 24-hr. precipitation stations in the United States.

2-yr. and 100-yr. 24-hr. maps (figs. 51 and 56). The values shown on the 2-yr. map are for the partial-duration series and are approximately 7 percent greater than those of the $\bar{x}$ map. The smoothed 100-yr. map is based on a combination of values from the $\bar{x}$ and $s_{x}$ maps, i.e., $x_{100} = \bar{x} + Ks_{x}$. By the Gumbel procedure the 100-yr. value is approximately the sum of the mean plus 3.5 standard deviations (fig. 4).

2-yr. and 100-yr. 1-hr. maps (figs. 16 and 21). An average 2-yr. 1-hr. to 2-yr. 24-hr. ratio of 0.36, based on three recording-gage stations, was applied to the $\bar{x}$ 24-hr. map to obtain the $\bar{x}$ 1-hr. map. The values shown on the 2-yr. map are for the partial-duration series and are approximately 7 percent greater than those of the $\bar{x}$ map. The coefficient of variation of the 1-hr. data was found to have an average value of 0.33. Multiplying the mean, $\bar{x}$, of the annual maximum values by 0.33 yielded values of the standard deviation, $s_{x}$. The 100-yr. 1-hr. map was then determined by adding 3.5 times the standard deviation to the mean annual maxima, or $x_{100} = \bar{x} + 3.5s_{x}$.

Additional isopluvial maps. The 2-yr. 1-hr., 2-yr. 24-hr., 100-yr. 1-hr. and 100-yr. 24-hr. maps were then used in conjunction with the duration and return-period relations of figures 2 and 3 to obtain 38 isopluvial maps for intermediate durations and return periods. The computations were made by a digital computer. Values were computed for and plotted on the grid of figure 5, and the isopluvials were then drawn with reference to these grid values. The seven 30-min. maps were developed from the relationship 0.75 times the values on the 1-hr. maps for corresponding return periods. The 49 rainfall-frequency maps are presented at the end of the text (figs. 8 to 56).

7. DEPTH-AREA RELATIONSHIPS

There are two basic types of depth-area relationships: (1) storm-centered relations, and (2) geographically-fixed relations. Storm-centered relations are derived from rainfall data in storm centers. The frequency-derived, geographically-fixed, depth-area curves of figure 6 are based on different parts of different storms instead of on the highest amounts surrounding the storm centers. Since the area is geographically-fixed, its rainfall stations measure rainfall sometimes near the storm center, sometimes on the outer edges, and sometimes in between the two. The averaging process results in the geographically-fixed curves being flatter than storm-centered curves. This is understandable considering that such curves are steeper near the centers of storms. Each type of curve is appropriate for its respective application—the storm-centered for PMP and the geographically-fixed for frequency data.

The depth-area curves of figure 6 are based on data from 20 dense raingage networks and are identical with those of Weather Bureau Technical Paper No. 29 series [5]. The ordinates of the 24-hr. curve, for example, are conveniently expressed as ratios (in percent) whose numerator is the average of the 2-yr. 24-hr. point values in the area.

8. SEASONAL VARIATION

The use of annual maxima (annual series) or $n$-maximum events for $n$ years of record (partial-duration series) for frequency analyses has been discussed. Obviously, some months contribute more events to these series than do other months, and some months may not contribute at all.
matter of interest the annual maximum 24-hr. data were analyzed to determine their monthly distribution. The diagram of figure 7 was developed from annual maximum 24-hr. rainfall data for 75 stations. All stations had at least 40 yr. of record, providing a total of 3963 station-years of data. These data were then classified according to month of occurrence and return period and summarized. The frequencies were computed for each month by determining the ratio (in percent) of the number of occurrences of amounts equal to or greater than the value for a particular return period to the total number of occurrences (years of record). Cases of non-occurrence as well as occurrence of rainfall events were considered in order to arrive at numerical probabilities. The probabilities were then plotted as a function of return period and season and smoothed isopleths fitted to the probabilities. Comparisons of seasonal probability curves based on annual maximum data with those based on partial-duration series data have not disclosed any appreciable differences.

The seasonal probability curves of figure 7 are based on stations scattered all over the Islands. There are various places in the Islands for which the curves are not representative. Attempts were made to construct different sets of curves for stations with a northeast exposure and for those with a southwest exposure. Some differences between the two sets of curves were noted, but they did not appear to be appreciable.
Figure 6.—Depth-area curves for rainfall-frequency data

Figure 7.—Monthly distribution (in percent) of 24-hr. annual maximum rainfalls for various return periods.

EXAMPLE: Determine the probability of occurrence of a 5-yr. 24-hr. rainfall for the months November through March. From figure 7, the probabilities for each month are interpolated to be 2, 3, 3.5, 2.5, and 3 percent, respectively. In other words, the probability of occurrence of a 5-yr. 24-hr. rainfall in November of any year is 2 percent; December, 3 percent; January, 3.5 percent; etc.
9. PROBABLE MAXIMUM PRECIPITATION (PMP)

The main purpose of PMP estimates is to provide complete-safety design criteria in cases where failure of a structure would be disastrous. Estimates of 6-hr. PMP are presented in figure 57. These estimates, taken from Hydrometeorological Report No. 39 [6], are based on a purely meteorological approach.

Ratio of 6-hr. PMP to 100-yr. 6-hr. point rainfall. The ratio of PMP to the 100-yr. rainfall provides a rough index of the geographic consistency and relative probability of the PMP estimates. In the United States the ratio for 6-hr. rainfall has been found [2] to range generally from 2 to 9. The low ratios are usually found in the wetter regions where the occurrence of high-intensity rainfalls is relatively common. The highest ratios are usually found in arid or semi-arid regions where high-intensity rainfalls are possible, but the probability of their occurrence is extremely low. This trend is found in the Hawaiian Islands. The ratio map of figure 58 shows the relative magnitude of the PMP estimates to be of the right order. The ratios range from about 1.5 to 7, the lowest ratios being on the windward slopes of Hawaii.

Depth-area curves. The PMP estimates of figure 57 are for point rainfall. These point values can be reduced for size of area by means of the depth-area curves of figure 59, which are merely another form of those presented in Hydrometeorological Report No. 39. These curves differ from those of figure 6 in that the former are storm-centered whereas the latter are geographically-fixed relations (see section on depth-area relationships above). The curves of figure 6 should be applied only to rainfall-frequency data, and those of figure 59, only to PMP estimates.

The two sets of depth-area curves show different rates of reduction for size of area. Extrapolation of the curves to appreciably larger areas than shown, and application to the respective index maps, would lead to PMP estimates smaller than the 100-yr. rainfall, patently unreasonable. Such extrapolation is not intended, and the depth-area relations are considered reliable over the ranges of area for which depicted. The largest natural watershed in the Islands suitable for development is about 100 sq. mi., most watersheds being much smaller. These areas are well within the critical limits, and no unusual problems are involved.

REFERENCES

Figure 9.—2 yr. 30-min. rainfall (in.)

2-YEAR 30-MINUTE RAINFALL (INCHES)
Figure 12.—25-yr. 30-min rainfall (in.)
Figure 45.—5-yr. 12-hr. rainfall (in.)
Figure 55.—50-yr. 24-hr. rainfall (in.)
Figure 58. - Ratio of probable maximum 6-hr. precipitation to 100-yr. 6-hr. rainfall (figs. 57 and 42).
Example: Determine hourly increments of 12-hr. PMP for a 30-sq. mi. watershed located on Oahu at 21°30' N., 158°00' W. Figure 57 indicates a 6-hr. point PMP of 24 in. for that location. For 30 sq. mi., figure 59 yields reduction factors for 1, 2, 3, 6, 9, and 12 hr. of 36, 52, 64, 88, 106, and 119 percent, respectively. Multiplying 24 in. by these factors yields 8.6, 12.5, 15.4, 21.1, 25.5, and 28.8 in. Plot these amounts against their respective durations to obtain the depth-duration curve of PMP for 30 sq. mi. Hourly increments of PMP read from this curve would be 8.6, 3.9, 2.9, 2.2, 1.8, 1.7, 1.6, 1.5, 1.3, 1.2, 1.0, and 0.8 in.